

### Example 6-5

Fig. E6-5 shows a 50-hp, 120-V, 1800-rpm shunt DC motor. The armature resistance is  $0.1 \Omega$  and the field resistance is  $50 \Omega$ . Assume compensating windings have completely taken care of the armature reaction. Also, ignore mechanical, core and miscellaneous losses. Initially, the motor is running a constant-torque load and draws  $12 \text{ kW}$  from the source at  $1,500 \text{ rpm}$ . Assume  $\phi$ - $I_f$  relation is linear. If the field resistance is increased to  $60 \Omega$  using an adjustable resistance in series with the field winding, find the new steady-state armature current and speed, as well as the power loss in the adjustable resistance.

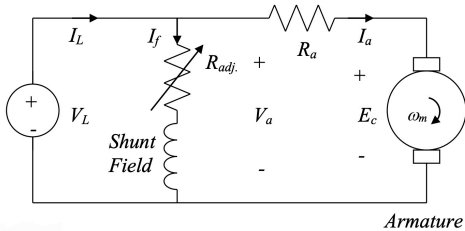


Fig. E6-5

Armature current before increasing resistance :

$$I_{a1} = I_{L1} - I_{f1}$$

$$P_{in} = 12000 \text{ W} = V_L I_{L1}$$

$$I_{L1} = \frac{12000}{120} = 100 \text{ A}$$

$$I_{f1} = \frac{V_L}{R_{f1}} = \frac{120}{50} = 2.4 \text{ A}$$

$$\therefore I_{a1} = I_{L1} - I_{f1} = 100 - 2.4 = 97.6 \text{ A}$$

Load torque is constant  $\rightarrow$  Developed torque in situation 2 = Developed torque in situation 1

$$T_{d1} = T_{d2}$$

$$K \phi_1 I_{a1} = K \phi_2 I_{a2}$$

$$I_{a2} = \frac{\phi_1}{\phi_2} I_{a1}$$

$\phi$  -  $I_f$  relation is linear :

$$\frac{\phi_1}{\phi_2} = \frac{I_{f1}}{I_{f2}} = \frac{V_L / R_{f1}}{V_L / R_{f2}} = \frac{R_{f2}}{R_{f1}} = \frac{60}{50} = 1.2$$

$$I_{a2} = \frac{\phi_1}{\phi_2} I_{a1} = 1.2 \times 97.6 = 117.12 \text{ A}$$